
A Bayesian decision theory approach for the techno-economic analysis of an all-optical router

**Víctor López¹, José Alberto Hernández¹, Javier Aracil¹, Juan
P. Fernández Palacios² and Óscar González de Dios²**

¹Universidad Autónoma de Madrid

²Telefónica I+D

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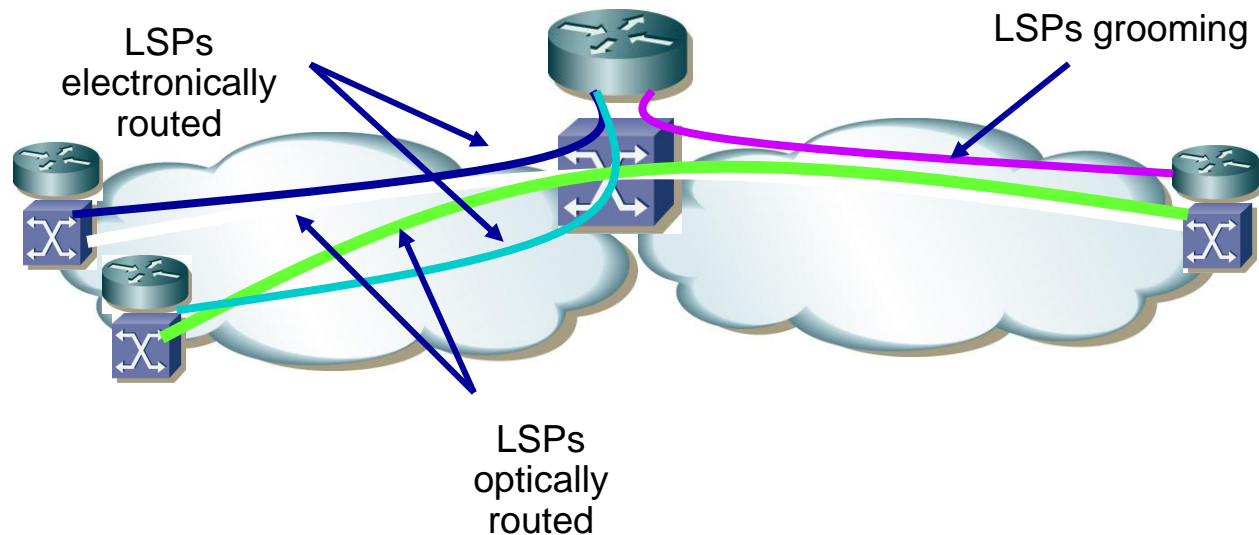
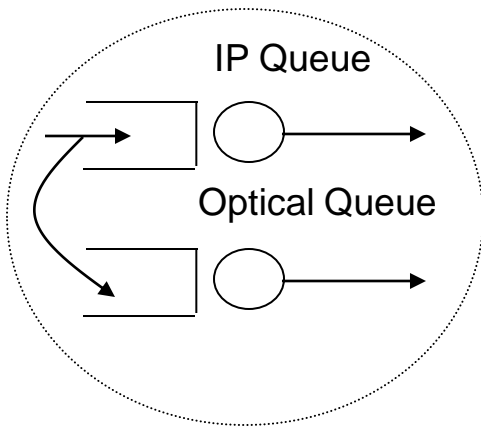
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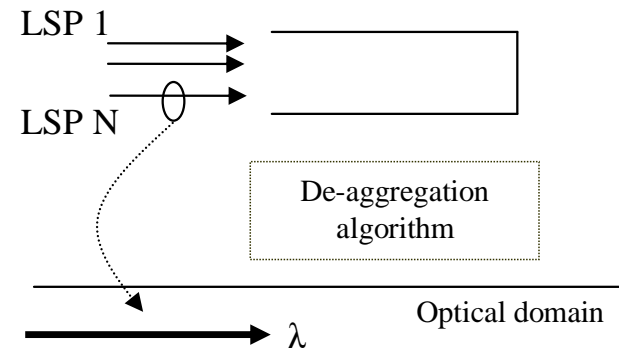
Multilayer scenario

- Current optical networks are migrating to an IP over WDM scenario.
- In such scenario, a multilayer-capable router has to decide whether to perform optical or electronic switching.



Multilayer scenario

- Which is the optimal decision to switch a new incoming LSP?
 - Electrical and optical resources vs. User Utility function



Proposal of a techno-economic model to help routers take the decision of optical or electronic switching of their LSPs.

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Techno-economic analysis

- There three key aspects in our model:
 - Bayesian theory.
 - Utility functions definition.
 - Cost function definition.

Bayesian decisor

- Let N refer to the number of LSPs handled at a given random time by the multilayer router, the loss function is given by:

$$L(d_i, \mathbf{x}) = (C_e(i) + C_o(N - i)) - U(\mathbf{x}), i = 1, \dots, N, \mathbf{x} > 0$$

- Where:
 - **$C_e(i)$ and $C_o(i)$** : cost associated to route i flows over the electrical or optical domain.
 - **$U(\mathbf{x})$** : utility associated to a queuing delay of x units of time, experienced by the electronically switched LSPs.

Utility function definition

- Definition:

- Utility associated to a queuing delay of x units of time, experienced by the electronically switched LSPs.

- Assumptions:

- The queuing delay is assumed to be Weibull distributed. [5-7]
- In this light the probability distribution function is :

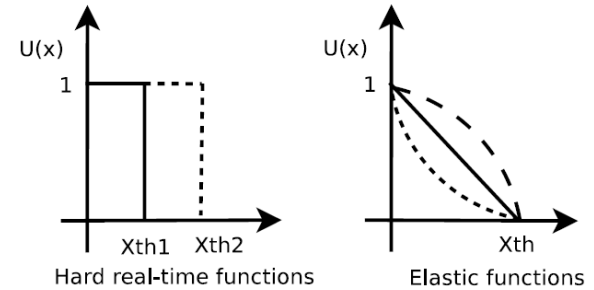
$$p(x) = (2-2H)C \frac{(C-m)^{2H}}{2K(H)^2am} (Cx)^{1-2H} \exp\left(-\frac{(C-m)^{2H}}{2K(H)^2am} (Cx)^{2-2H}\right)$$

– Where:

- » m : input traffic mean, H : Hurst parameter, $am = \sigma^2$.



Utility function definition



- We define three utility functions:
 - **Delay based utility**
 - The utility function is opposite to the queuing delay x .
 - **Hard real-time utility**
 - Hard real-time applications are those which tolerate a T_{\max} delay.
 - » ITU-T Y.1541 [10] and 3GPP S.R0035[11] defined service classes based on thresholds.
 - **Elastic utility**
 - Services, which are degraded little by little, till they reach T_{\max} .
 - » Exponential function used to describe the degradation of elastic services [9].
 - » G.107 “E model” [12], for voice service degradation.

$$U_{delay}(x) = -x$$

$$U_{step}(x) = \begin{cases} 1 & \text{if } x < x_p \\ 0 & \text{otherwise} \end{cases}$$

$$U_{exp}(x) = \lambda e^{-\lambda x}$$

$$\lambda = \frac{1}{T_{\max} \log(1 - 0.9)}$$

Cost function definition

- Definition:

- $C_e(i)$ and $C_o(N - i)$ represent the cost associated to switching i LSPs in the electronic domain and $N - i$ in the optical domain.

$$C_e(i) = Ki$$

$$C_o(N - i) = R_{\text{cost}}K(N - i)$$

- Where R_{cost} is the ratio at which the optical cost increases with respect to the electronic cost.

Bayes risk

- The Bayes risk equals:

$$R(d_i) = E_x[L(d_i, x)] = (C_e(i) + C_o(N - i)) - E_x[U(x)]$$

- The goal is to obtain the optimal decision d^* such that the Bayes risk $R(d^*)$ is minimum:

$$\text{find } d^* \text{ such that } R(d^*) = \min_{d_i, i=1, \dots, N} R(d_i)$$

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Experiments and results

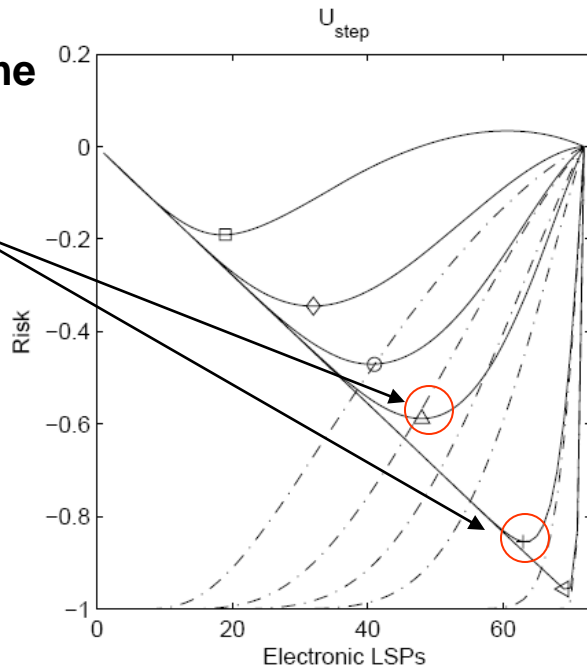
- Scenario:
 - 2.5 Gbps core network link.
 - $N = 72$ standard VC-3 LSPs ($m = 34.358$ Mbps).
 - Hurst parameter: $H = 0.6$ [13]
 - $a = \sigma/m = 0.3$.
 - $K = 1/N$, to normalized electrical cost in range $[0, 1]$.
- Experiments:
 1. Range of QoS (T_{\max})
 2. Range of cost (R_{cost})
 3. Range of Self-similarity (Hurst parameter)

QoS parameters

- T_{\max} variation from 0.1 ms to 100ms.*
 - Optically-switched LSPs increase with T_{\max} .
 - Delay requirements for hard real-time applications are tighter than those for elastic applications.

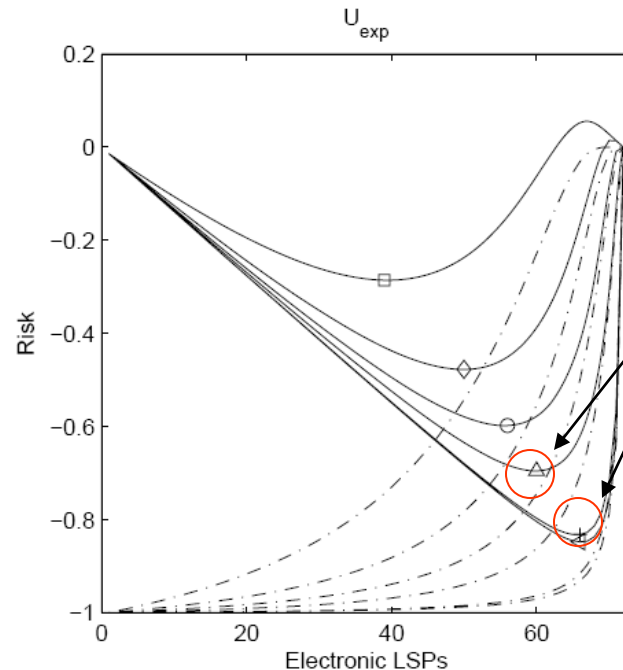
Hard real time

d_{48} -1ms and
 d_{63} -10ms



Elastic apps

d_{60} -1ms and
 d_{66} -10ms



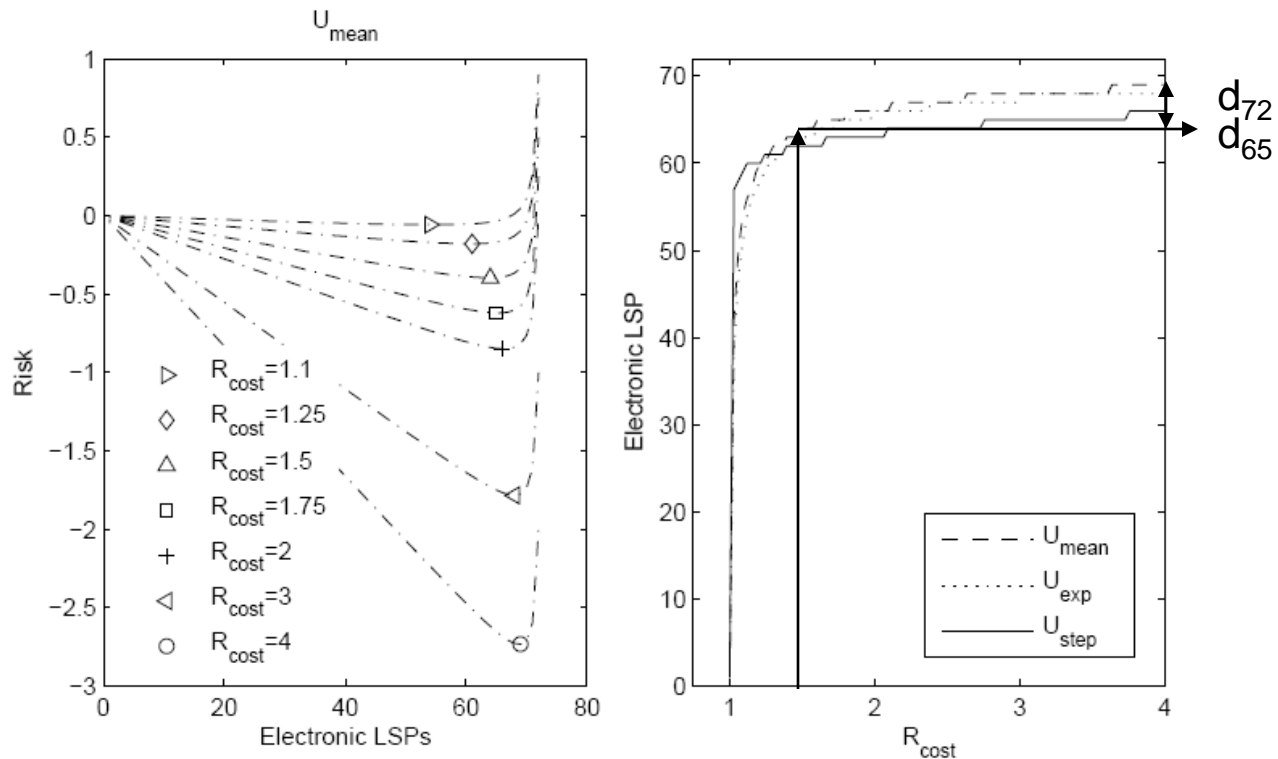
□ $T_{\max}=0.1\text{ms}$
◇ $T_{\max}=0.25\text{ms}$
○ $T_{\max}=0.5\text{ms}$
△ $T_{\max}=1\text{ms}$
+ $T_{\max}=10\text{ms}$
◁ $T_{\max}=100\text{ms}$



* $R_{\text{cost}}=2$

Cost variation

- R_{cost} variation from 1.1 to 4.*
 - The more expensive optical switching is the less number of LSPs are switched optically.
 - If $R_{\text{cost}} \geq 1.5$, the optimal decision does not depend on other parameters.



* $T_{\text{max}}=10\text{ms}$

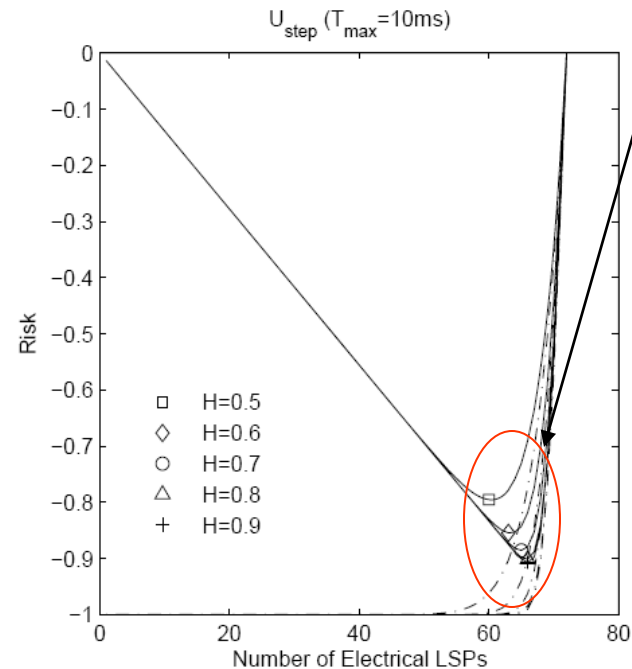
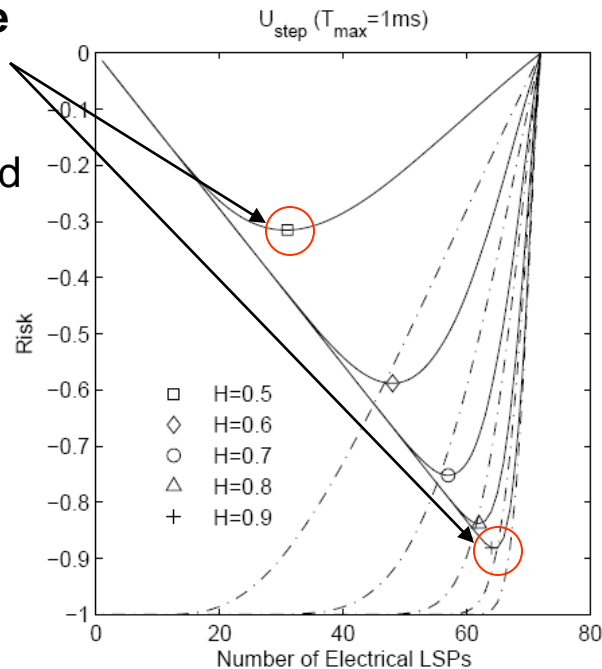


Self-similarity

- Hard real time applications:
 - H variation from 0.5 to 0.9.*
 - Incoming traffic characteristics impact on the bayesian decisor depends on the QoS parameters.
 - In Hard real time with T_{max}=1ms has no impact.

Hard real time
T_{max}=10ms

d₃₁ – H=0.5 and
 d₆₄ – H=0.9



Hard real time
T_{max}=1ms

Almost no difference



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Contributions

- Novel methodology based on the Bayesian decision theory for multilayer switching decision, QoS parameters and cost.
- The algorithm proposed is of low complexity, and can easily adapt to changing conditions.
- Future work:
 - Extensions of this mechanism, using end-to-end delay information through the whole network.



Thank you!!
Questions?

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